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# Stochastic averaging of quasi partially integrable Hamiltonian systems under fractional Gaussian noise

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**Key words:** Fractional Brownian motion (fBm); Fractional Gaussian noise (fGn); Quasi partially integrable Hamiltonian system; Stochastic averaging method; Stationary response

# ◆ Fractional Guassian noise (fGn)

- Many real excitations in nature have property of long-range spatial and/or temporal correlations (long memory). These excitations can be modeled as fGn.
- FGn has already been applied as excitation model in physics, finance, and biology, etc.

characteristics

- self-similarity
- long range dependence (see Fig.1: Auto-correlation function  $R(\tau)$  of fGn)

- The response of dynamical system to fGn is not Markov process.

Hurst index of fGn  $\longrightarrow 1/2 < H < 1$

- The power spectral density(PSD) of fGn is meaningful physically only when  $1/2 < H < 1$ . Thus, only  $1/2 < H < 1$  is considered in this paper. (see Fig.1: PSD  $S(\omega)$  of fGn)

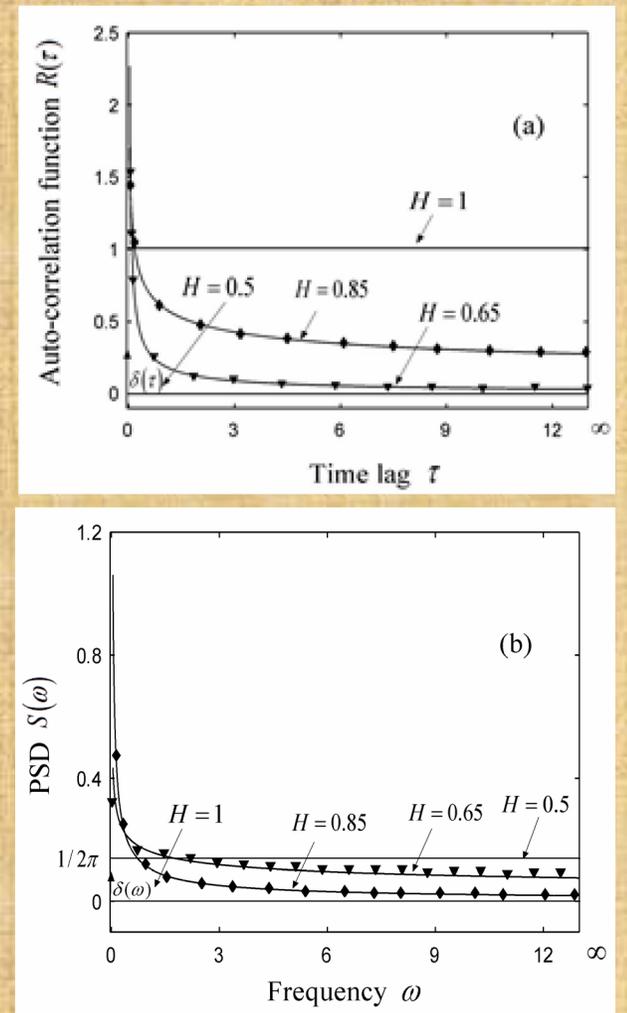
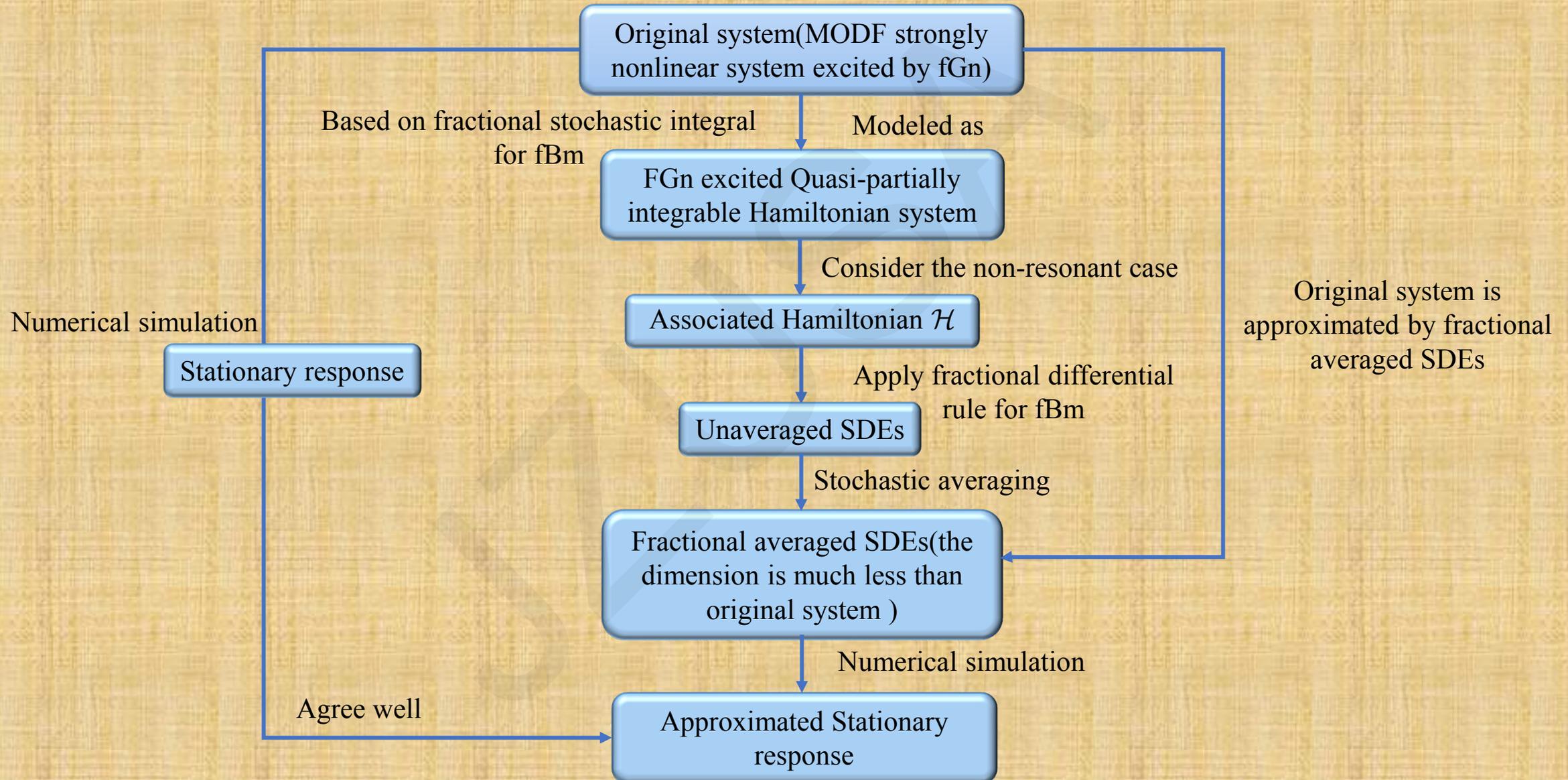


Fig. 1 Auto-correlation function  $R(\tau)$  (a) and PSD  $S(\omega)$  (b) of fGn  $W^H(t)$  with the simulated results ( $\nabla$   $\blacklozenge$  indicate simulated results)

# ◆ Stochastic averaging method



## ◆ Results and conclusion

- Two examples are worked out to illustrate the proposed stochastic averaging method.

### Advantages

- ◆ **Effectiveness:** The probability density and statistics of first integrals calculated from averaged SDEs and those from the original system agree well while the error is acceptable.
- ◆ **Efficiency:** The dimension of the original system is greatly reduced. Thus, the computation time for simulating averaged fractional SDEs is much less than that for original system.

- Thus, in the future, it is promising to apply the proposed averaging method to do more study work.