

## Simulation analysis of fracture process of slag deposits surrounding wall tubes during steam sootblowing\*

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**Abstract:** The slag deposited on the wall tubes of furnaces/boilers seriously reduces the heat transfer from the furnace to tubes and degrades the tubes by corrosion. During boiler operation, slag deposits are removed by sootblowers that blast the deposits with steam or air jets. In this study, we develop a novel numerical model using the cohesive zone method (CZM) and coupled Eulerian–Lagrangian (CEL) analysis to investigate the dynamics and mechanism of deposit fracture during sootblowing. Cohesive elements subject to the softening traction–separation relationship and evolution laws are embedded into the deposit model to describe crack formation during deposit breaking. The deposit cracking status is evaluated by extracting the scalar stiffness degradation variable from damaged cohesive elements. The dynamic process and mechanism of deposit fracture are analyzed and revealed in detail, particularly in terms of the destructive degree and fracture rate of the deposit model. The effects of the sootblowing steam pressure (0.9–1.8 MPa) on slag breaking, wall tube stress, and steam consumption are also investigated. Sootblowing steam pressures over 1.2 MPa do not further benefit the sootblowing effect but adversely affect the wall tube lifetime.

**Key words:** Sootblowing; Boiler; Numerical model; Cohesive zone method (CZM); Deposit fracture  
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### 1 Introduction


The accumulation of fireside deposits can be a problem in boilers all over the world (Fan et al., 2001). Slag deposits on water wall tubes not only reduce the heat transfer efficiency in boilers but also degrade steam tubes by corrosion (Žbogar et al., 2006). Sootblowing is an effective and conventional method to overcome this problem, and it can be performed using high-pressure steam, air, or sound waves. Deposit

fracture caused by sootblowing is a complex mechanical process that includes the aerodynamic aspects of the sootblower jet and the breaking of the slag layer.

Previous studies at the University of Toronto, Canada (Jameel et al., 1994; Kaliazine et al., 1997, 1999) discussed sootblower jet dynamics and solid deposit removal mechanics. The effects of the deposit strength and thickness and sootblower jet characteristics on deposit removal were also investigated. In this regard, Pophali et al. (2009, 2013) used gypsum to simulate brittle deposits. They also performed many lab-scale experiments in which cylindrical gypsum deposits were exposed to a supersonic air jet. They obtained fundamental information on sootblower jet dynamics and the interactions between the sootblower jet and the deposits. The results showed

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that brittle deposits could be destroyed within a short blowing time (nearly 3 ms). Moreover, they developed a computational fluid dynamics model to predict the flow behavior of sootblower jets (Busmann et al., 2013; Doroudi et al., 2014).

However, replicating the actual process of deposit failure through experiments is difficult due to the complexity of accurate observation of the furnace environment and slag properties. Coal ash deposits are usually assumed as brittle materials, which can be fractured by a sootblower jet (Ebrahimi-Sabet, 2001). With rapid developments and innovations in computer-aided engineering technology in recent years, several methods such as the finite element method (FEM) have been increasingly applied to replicate the process of brittle material breaking. Furthermore, the cohesive zone method (CZM) has been used extensively in predicting the fracture behavior of brittle materials. In this regard, Guo (2014) investigated a 3D fracture model through a combined finite-discrete element method and cohesive crack model. The author also discussed the sensitivity of mesh size and orientation to numerical results in another study (Guo et al., 2016). Jiang and Meng (2018) developed a 3D numerical model of rock breaking using a hybrid finite and cohesive element method to stimulate rock fracture and chip formation. Yao (2012) developed a 3D pore pressure CZM to predict crack initiation and growth in quasi-brittle materials considering the material softening effect. The author subsequently applied the model to predict hydraulic fracturing under fluid injection. Gálvez et al. (2002) presented a numerical procedure for mixed-mode fracture of quasi-brittle materials, whose mode is based on the cohesive crack approach. Their numerical results agreed relatively well with two experimental sets of mixed-mode fractures of concrete beams. Elices et al. (2002) indicated that the CZM could adequately predict the behavior of uncracked structures. This model, which was initially applied to concrete and cementitious composites, can also be successfully used for other materials such as polymer and certain steels.

In summary, numerical fracture models based on the CZM of brittle materials such as rock, ceramics, gypsum, and concrete have been generally developed and applied. The results of numerical fracture models based on the CZM have presented good agreements with experiments in the literature (Turon et al., 2007; Awinda et al., 2016; Gui et al., 2016; Jiang and Meng,

2018). However, this new simulation method has not thus far been applied to study ash deposit fracture in coal-fired boilers; previous studies have usually experimentally discussed the overall results of ash deposit removal by sootblowing. To replicate the ash deposit failure dynamically and comprehensively, we develop a novel 3D numerical model that combines the CZM and coupled Eulerian–Lagrangian (CEL) analysis in this study, and we consider all aspects of interest including ash deposit, wall tube, and sootblowing steam in the simulations. This new simulation study can contribute to a better understanding of the dynamics and detailed characteristics of the ash deposit fracture process, which have not been revealed thus far by experiments. The dynamic process of deposit fracture is revealed in detail, and the diffusion of the steam jet and spread of the stress wave in deposits are also analyzed. The sootblowing steam pressure is investigated to discover its effects on slag breaking, wall tube stress, and steam consumption.

## 2 Methods

### 2.1 CZM approach

The CZM in ABAQUS FE software adopted in this study is based on the model developed by Hillerborg et al. (1976). Cohesive elements can simulate several types of behavior at interfaces when the interface load-carrying capability is lost (Chen et al., 2009). The available traction–separation model in this approach initially assumes linear elastic behavior with nominal stress and strain quantities, followed by the evolution of damage. The typical traction–separation responsible for a single mode is defined by two points for the normal direction, that is, the onset of damage ( $\delta_n^o, t_n^o$ ) and complete decohesion ( $\delta_n^f, 0$ ) (May, 2015), as shown in Fig. 1, where  $t_s$  and  $t_t$  represent the shear components of traction, and  $\delta_s$  and  $\delta_t$  are the shear components of separation. The relative displacement at damage initiation,  $\delta_n^o$ , for the normal direction is expressed as

$$\delta_n^o = \frac{t_n^o}{K_n}, \quad (1)$$

where  $t_n^o$  denotes the stress at initiation, and  $K_n$  is the element stiffness.

With the application of the maximum nominal stress criterion in this study, damage is assumed to be initiated when the maximum nominal strain ratio reaches a value of 1 (Awinda et al., 2016). This criterion can be represented as

$$\max \left\{ \frac{\langle t_n \rangle}{t_n^0}, \frac{t_s}{t_s^0}, \frac{t_t}{t_t^0} \right\} = 1, \quad (2)$$

where  $\langle \rangle$  represents the Macaulay bracket with the usual interpretation. These brackets are used to signify that a pure compressive deformation or stress state does not initiate damage. Therefore,  $\langle t_n \rangle = t_n$  when  $t_n > 0$ ; otherwise,  $\langle t_n \rangle = 0$ .

Damage evolution describes the rate of degraded material stiffness once the initiation criteria are met. In addition, zero normal and shear stiffnesses exist when the interface is fully destroyed under tension or full fracture opening (Gui et al., 2015). Scalar stiffness degradation variable  $D$  is proposed to represent the overall damage. This variable can also evolve from 0 to 1 with further loading after damage initiation (Jiang and Meng, 2018). Parameter  $D$  can be presented as follows for the normal direction (Camanho and Dávila, 2002; Kazerani et al., 2012):

$$t = \begin{cases} K \delta_n, & \delta_n \leq \delta_n^0, \\ (1-D)K \delta_n, & \delta_n^0 < \delta_n < \delta_n^f, \\ 0, & \delta_n \geq \delta_n^f, \end{cases} \quad (3)$$

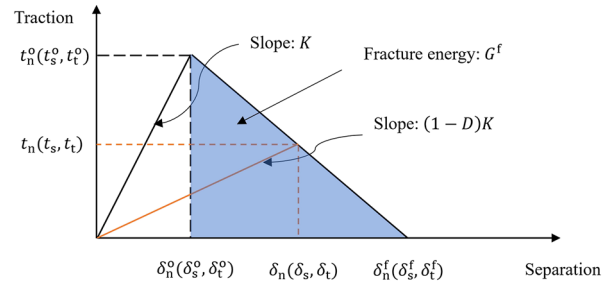
$$D = \frac{\delta_n^f (\delta_n - \delta_n^0)}{\delta_n (\delta_n^f - \delta_n^0)}, \text{ and } 0 \leq D \leq 1, \quad (4)$$

where  $K$  denotes the stiffness that relates the nominal stress to the displacement in CZM.  $D$  denotes an essential and a necessary variable to measure the extent of deposit failure in our study, and its meaning in the traction–separation curve is depicted in Fig. 1. Parameter  $\delta^f$  denotes the displacement among adjoining elements when the material completely fails. This variable is defined on the basis of Griffith's theory (Griffith, 1921), which assumes that fracture energy  $G^f$  is absorbed during the formation of the fracture surface. Parameter  $G^f$  denotes a material property that corresponds to the shaded area under the traction–displacement curve in Fig. 1. In addition, fracture energy  $G^f$  can be expressed as (Guo, 2014)

$$G^f = \int_{\delta^0}^{\delta^f} t d\delta \approx \frac{1}{3} t^0 \delta^f. \quad (5)$$

Therefore, failure displacement  $\delta^f$  can be defined as

$$\delta^f = 3 \frac{G^f}{t^0}. \quad (6)$$



**Fig. 1** Typical traction–separation response and damage response in cohesive zone method (CZM)

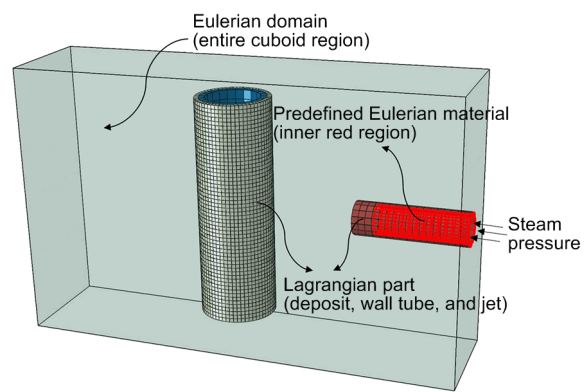
## 2.2 CEL analysis method

CEL is an effective method to solve unstable fluid–structure coupling surface problems, and it allows immediate transfer of the parameters between Eulerian and Lagrangian domains. This coupled approach can achieve the interaction of Eulerian and Lagrangian bodies within a model domain in ABAQUS. Thus, it is convenient to observe the dynamic process of steam-flow-coupled deposit fracture at the same time.

In the traditional Lagrangian analysis, nodes are fixed within the material, and the elements deform with the material. Lagrangian elements are consistently 100% full of a single material. Thus, the material boundary coincides with an element boundary. The deposit and wall tube model are based on Lagrangian analysis in this study. In contrast, in Eulerian analysis, the nodes are fixed in space, and materials flow through elements that do not deform. Eulerian elements may not consistently be 100% full of a single material. Therefore, the Eulerian material boundary must be computed during each time increment, and it does not correspond to an element boundary. If any Eulerian material moves outside the Eulerian mesh, then the material is lost from the simulation (ABAQUS, 2016). The high-temperature steam component is based on the Eulerian analysis in this study.

Fig. 2 presents the diagrammatic sketch of the entire CEL model including the Eulerian and Lagrangian regions. We first construct a cuboid Eulerian domain (meshed by Eulerian elements) containing all Lagrangian parts (meshed by Lagrangian elements including the deposit, wall tube, and jet). In the Eulerian domain, material assignment relies on the parameter of material volume fraction that is in the range of 0–1.0. The material volume fraction represents the percentage of the element's volume that is occupied by the given Eulerian material. A fraction value of 1.0 indicates that the region is completely filled with the Eulerian material (ABAQUS, 2016). In our simulation, the initial Eulerian material, steam, was assigned originally inside the jet nozzle (inner red region), and the volume fraction was zero in the Eulerian domain except in the inner red region. During the CEL analysis, the Eulerian material (sootblowing steam) was pressed and ejected from the nozzle continuously, and subsequently, ABAQUS tracked the Eulerian material in each element via calculating the volume fractions. When the Eulerian material interacted with the Lagrangian material (ash deposit), the stress on the deposit caused by steam impact was calculated according to the penalty method, which is the Eulerian–Lagrangian contact method in ABAQUS.

(element type: C3D8R) by a Python program. The C3D8R element was an eight-node linear brick with reduced integration and hourglass control, and this element type could prevent locking phenomena due to the reduced integration in ABAQUS. Note that linear elements should be chosen instead of quadratic elements, because the lumped mass method used with the linear elements is more effective in simulating the stress wave propagation than the consistent mass method used with the quadratic elements (ABAQUS, 2016).



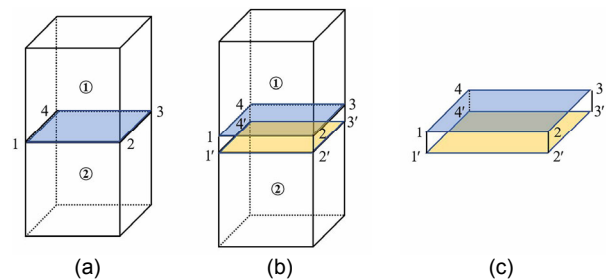
**Fig. 2 Diagrammatic sketch of the entire CEL model**

Note: for interpretation of the references to color in this figure, the reader is referred to the web version of this article

### 3 Numerical model and analysis

#### 3.1 Cohesive zone modeling procedure

To realize the CZM approach, a certain type of element (i.e. cohesive elements with softening traction–separation relationship) and evolution laws were implemented among the solid elements in the initial mesh to model potential cracks (Su et al., 2010a, 2010b). In Fig. 3, two adjacent hexahedral elements (Fig. 3a) are considered as examples to clarify the procedure of embedding a zero-thickness eight-node cohesive element. The shared interface (i.e., nodes 1, 2, 3, and 4) between both adjacent hexahedral elements (① and ②) is replaced by an eight-node cohesive element (added new nodes 1', 2', 3', and 4') with zero thickness, as shown in Fig. 3b. Fig. 3c shows the detailed structure of the eight-node cohesive element. Such cohesive elements (element type: COH3D8) were automatically inserted into the deposit model



**Fig. 3 Schematic of insertion of eight-node cohesive element between two hexahedral elements**

(a) Two adjacent hexahedral elements; (b) Insertion of eight-node cohesive element; (c) Detailed structure of the cohesive element

#### 3.2 Modeling of deposit and sootblower jet

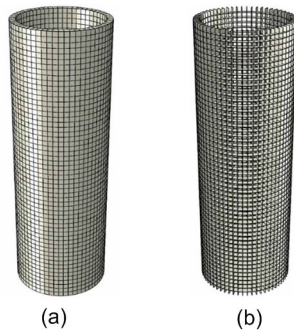
In this study, FEM was implemented using ABAQUS/Explicit to simulate the sootblower jet dynamics and deposit failure. The type of sootblower selected in this study was the IR-3Z developed by the Diamond-Power Company, USA. Fig. 2 displays the

diagrammatic sketch of the model, in which a wall tube and its slag deposit on the surface along with the sootblower jet nozzle are emphasized. Table 1 lists other relevant parameters of the object model. The distance between the sootblower jet nozzle and the deposit was set as 78 mm in this model.

Fig. 4 shows the insertion of zero-thickness cohesive elements among the adjacent solid elements in the deposit model. Cracks can initiate and extend these inserting elements when the maximum nominal stress criterion is satisfied.

**Table 1** Relevant parameters used in the model

Parameter	Value
External diameter of jet (mm)	30
Internal diameter of jet (mm)	25.4
Length of sootblower jet (mm)	100
External diameter of wall tube (mm)	60
Internal diameter of wall tube (mm)	50
Height of wall tube (mm)	200
Thickness of deposit (mm)	4



**Fig. 4** Numerical model for deposit cracking: (a) deposit model; (b) embedded cohesive elements

The most important property concerning ash deposit removal is the tensile strength because deposits can break at their weakest point (Zbogor et al., 2009). Moreover, the tensile strength of the deposits is influenced by the deposit chemical composition, thickness, and porosity (Kaliazine et al., 1997). In this study, the tensile strength of the ash deposit was assumed as that corresponding to the onset of damage stress,  $t^0$ , mentioned in the CZM because deposit damage was assumed to initiate when the stress on the deposit surface was greater than the tensile strength. Elastic properties are also relevant for deposit be-

havior, including Poisson's ratio and the elastic (Young's) modulus. For Poisson's ratio, the value range of 0.20–0.25 was acceptable in this study, similar to the range of most types of glass and ceramic (Wain et al., 1991). The elastic (Young's) modulus presents the relative stiffness within the elastic range (Zbogor et al., 2009), and it determines the initially linear elastic behavior with nominal stress and strain quantities in the traction–separation curve. The elastic modulus of porous-like material deposits ( $E$ ) can be related to the elastic modulus of nonporous materials (Wain et al., 1991) via the Mackenzie relationship (developed for ceramic porous materials):

$$E = E_0(1 - ap + bp^2), \quad (7)$$

where  $E_0$  represents the elastic modulus of nonporous materials,  $p$  is the porosity of porous materials, and  $a$  and  $b$  are the pore shape factors of porous materials.

The parameters of the CZM included Young's modulus ( $E$ ), tensile strength ( $t^0$ ), and failure displacement ( $\delta^f$ ). Previous studies (Kaliazine et al., 1997; Zbogor et al., 2009) have shown that the tensile strength and Young's modulus of the ash deposits depend strongly on the deposit porosity. The porosity of a typical coal deposit is 20%, and the tensile strength and Young's modulus were obtained according to their relationships with porosity as reported in the literature (Kaliazine et al., 1997; Zbogor et al., 2009). Failure displacement ( $\delta^f$ ) was calculated by means of Eq. (6) according to Guo (2014); the results are listed in Table 2. The most common material of boiler wall tubes is low-carbon steel (such as No. 20 steel), whose properties are also included in Table 2.

The properties of the sootblower steam material were modeled using the  $U_s$ – $U_p$  equation of state materials in ABAQUS. This equation is also called the Mie–Grüneisen equation, and it describes the linear relationship between shock and particle velocities, as follows:

$$U_s = c_0 + sU_p, \quad (8)$$

where  $U_s$  is the shock velocity,  $U_p$  is the particle velocity,  $c_0$  denotes the speed of sound in the fluid material, and  $s$  is the material constant (Smojver and



Ivančević, 2011). The relationship between pressure  $p$  and density  $\rho$  can be defined as (ABAQUS, 2016)

$$p = \frac{\rho_0 c_0^2 \eta}{(1 - s\eta)^2} \left( 1 - \frac{\Gamma_0 \eta}{2} \right) + \Gamma_0 \rho_0 E_m, \quad (9)$$

where  $\rho_0$  represents the initial material density,  $\eta = 1 - \rho_0/\rho$  is the nominal volumetric compressive strain,  $\Gamma_0$  is the material constant, and  $E_m$  is the internal energy per unit mass (Smojver and Ivančević, 2011). Parameters  $s$  and  $\Gamma_0$  are set to zero to provide a simple hydrostatic bulk response (Chizari et al., 2009). The main properties of steam are as follows: density,  $\rho_0 = 1.46 \text{ kg/m}^3$ ; steam temperature,  $T = 600 \text{ K}$ ; working pressure of steam,  $P_0 = 0.4 \text{ MPa}$ ; acoustic speed in the material,  $c_0 = 597 \text{ m/s}$ .

**Table 2** Properties of the deposit and wall tube adopted in simulation (Kaliazine et al., 1997; Zbogor et al., 2009; Guo, 2014)

Property	Value	
	Deposit	Wall tube
Density, $\rho$ (kg/m <sup>3</sup> )	2700	7900
Young's modulus, $E$ (MPa)	$1.0 \times 10^4$	$7.9 \times 10^5$
Poisson's ratio, $\nu$	0.25	0.3
Porosity (%)	20	—
Tensile strength, $t$ (MPa)	5	—

## 4 Results and discussion

### 4.1 Mesh independence analysis

The mesh accuracy of the deposit model is an important factor in determining the correctness of the simulation results, including the shape of cracks and failure time of the deposit. Although a fine deposit mesh can enhance the rationality and precision of the concerned modeling, the calculating time can also increase.

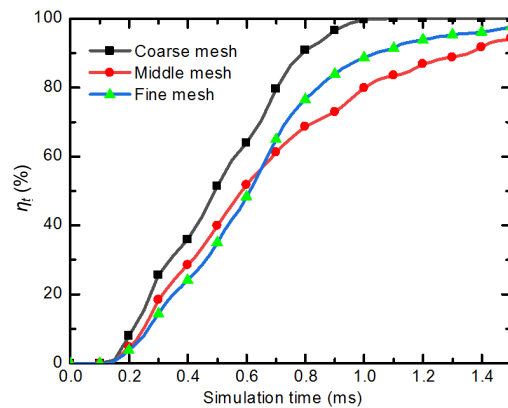
The scalar stiffness degradation variable  $D$ , as described in Eqs. (3) and (4), was adopted in this study to measure mesh independence. Fig. 1 illustrates the significance of  $D$ . After ABAQUS completed the calculations, the output database files were post-processed to extract the number of damaged cohesive elements from each output dataset of the deposit model. In addition, deposit zones were considered entirely damaged if the value of  $D$  was over 0.9 in cohesive elements. The fracture of the cohesive

elements became increasingly severe as the value of  $D$  approached 1. The destructive degree of the deposit model can be defined as

$$\eta_t = \frac{N_t^{0.9}}{N_{\text{total}}} \times 100\%, \quad (10)$$

where  $N_t^{0.9}$  denotes the number of cohesive elements whose value of  $D$  exceeds 0.9 at time  $t$ ;  $N_{\text{total}}$  is the sum of the number of cohesive elements, which is a constant number if the cohesive elements are embedded into the deposit model;  $\eta_t$  is the parameter that measures the destructive degree of the deposit at time  $t$ . Therefore, the closer the value of  $\eta_t$  is to 100%, the more severe is the damage degree in the deposit model.

In mesh dependency analysis, three different mesh sizes (i.e. coarse, middle, and fine meshes with 3318, 6667, and 9044 cohesive elements, respectively) were compared via the value of  $\eta_t$ , which changes with the simulation time (1.5 ms). In addition, the value of the sootblowing pressure was assumed as 1.2 MPa in the three cases, as shown in Fig. 5. We note that the  $\eta_t$ -time curve trends with middle and fine meshes are roughly similar. In comparison with the cases of the middle and fine meshes, the deposit with the coarse mesh is easily destroyed and breaks entirely at 1 ms. Meanwhile, approximately 80% of the middle and fine cases are observed to be destroyed simultaneously. However, the elements contained in the coarse mesh can be easily distorted excessively upon high-temperature steam impact, which leads to non-convergence of the results. In view of the calculating time cost, convergence, and mesh precision, the middle mesh size was selected in this study.



**Fig. 5** Mesh dependency analysis of three different sizes of deposit mesh (steam pressure is 1.2 MPa)

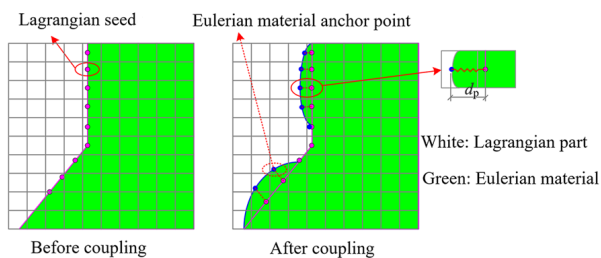
## 4.2 Sootblower steam flow and deposit-breaking process

To describe the contact at the interface between the Eulerian and Lagrangian domains, we used the penalty method in ABAQUS. Seeds were created at the Lagrangian element edges and faces while anchor points were created on the Eulerian material surface (Benson and Okazawa, 2004; Qiu et al., 2011). The penalty method allowed small penetration of the Eulerian material into the Lagrangian domain, as shown in Fig. 6. Contact force  $F_p$ , which was enforced between the seeds and anchor points, was proportional to penetration distance  $d_p$ , as expressed in Eq. (11):

$$F_p = k_p d_p, \quad (11)$$

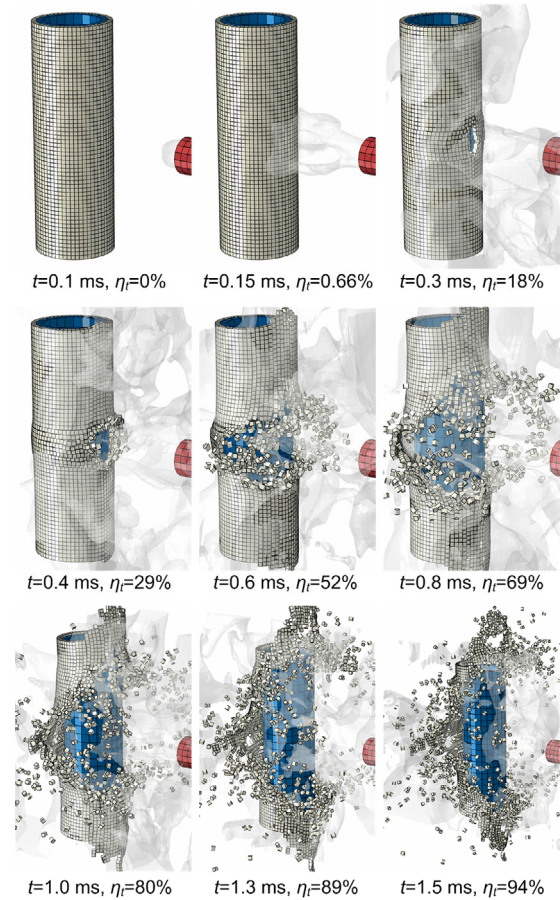
where the factor  $k_p$  denotes the penalty stiffness that depends on the Lagrangian and Eulerian material properties. Contact force  $F_p$  was regarded as the compressive force impressed on the deposit from the steam jet.

Deposit failure and chip formation during deposit breaking by steam flow sootblowing were simulated at a sootblowing pressure of 1.2 MPa. The interval time between output images was 0.05 ms, and the total simulation time was 1.5 ms, which was sufficient to express the details of the deposit changes. The failure time of the deposit coincided with certain research results (Pophali et al., 2013). Fig. 7 illustrates the dynamic results of the deposit-cracking process during sootblowing, including variations in the high-pressure steam flow, fracture zone of the deposit, and values of  $\eta_t$ . Fig. 8 reveals the  $D$  values of the cohesive elements inserted to observe their dynamic changes during the simulation.

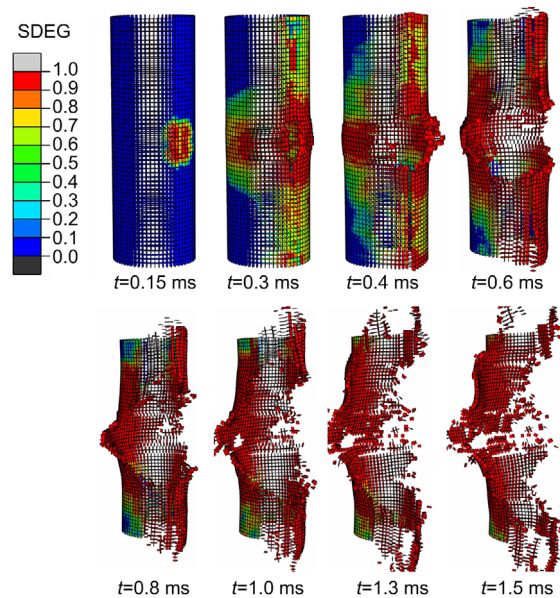


**Fig. 6** Definitions corresponding to penalty method

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**Fig. 7** Dynamic results during sootblowing processes



**Fig. 8** Value of scalar stiffness degradation variable (SDEG,  $D$ ) of inserted cohesive elements at different times

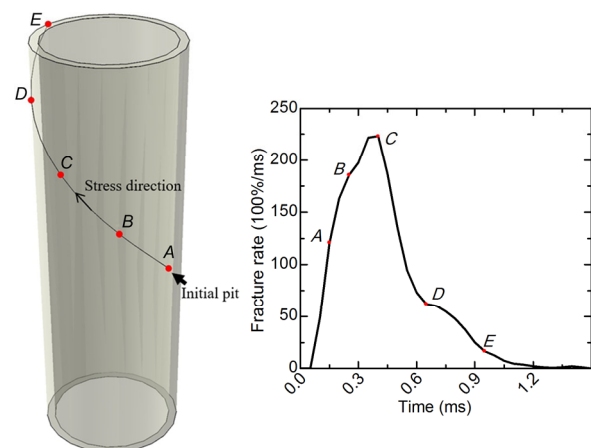
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As shown in Fig. 7, the steam flow is translucent. This result is in accordance with practical scenarios, and it is beneficial to investigate the overall process of crack formation directly. The steam flow ejected from the sootblower nozzle can be observed when the time is 0.1 ms. In the next 0.05 ms, the steam flow immediately interacts with the deposit layer. The initiation of microscopic cracks in the deposit zone under steam pressure is observed at 0.3 ms, and the value of  $\eta_t$  reaches 18% at this time. Corresponding to the same time instant in Fig. 8, the cohesive elements of the deposit/steam contact area are already destroyed, and the stress wave gradually spreads at 0.3 ms. The area of the destroyed deposit presents a rapid growth at 0.4 ms, and the maximum amount of deposit is ruptured at 1 ms, with the value of  $\eta_t$  reaching 80%. The steam flow gradually diffuses the entire Eulerian domain modeled previously, and when the jet contacts the brittle deposit, it shatters the deposit into pieces. As shown in Fig. 8, the red area of the cohesive elements indicate severe deposit damage, and the damaged deposit area slightly changes from 1.0 ms to 1.5 ms. The reverse sides of the deposit near the edge cannot easily be compressed and wrecked under steam impact. The value of  $\eta_t$  reaches 94% at the end of the simulation. Therefore, nearly all areas in the deposit model are destroyed.

In this study, the deposit material properties were independent of the microstructure details and considered as isotropic. The sootblowing jet imposed a large compressive force on the deposit when it impacted the surface of the deposit, and subsequently, the deposit elements were squeezed and deformed in the transverse direction. Transverse deformation produced transverse normal tension on the cohesive elements, and cracks occurred when the normal tension was greater than the tensile strength ( $t^0$ ).

Fig. 9 shows the calculated fracture rate of ash deposit,  $d\eta_t/dt$ . The figure also presents the onsite fracture time of five equidistant points (A, B, C, D, and E) on the deposit surface. When the initial pit is formed at point A due to jet impingement, a transverse normal tension is simultaneously generated. Thereafter, the tension wave spreads quickly in the deposit from point A, which leads to acceleration of the fracture rate accompanied with the sootblowing jet impact, as implied by the right-hand portion of the  $d\eta_t/dt$  curve from point A to point C. After the rate

reaches the peak at 0.4 ms, over 50% of deposit is broken, and the fracture rate begins decreasing because the rear portion of the deposit is not directly impacted by the steam jet, as indicated in the curve from point C to point E. The deposit is finally broken at E without steam impact due to stress wave propagation. In summary, the spread of the transverse normal tension caused by the steam jet primarily contributes to the deposit fracture, and further, direct steam impact on the deposit forms the initial source of transverse normal tension and plays a subsidiary role after initiation of the deposit fracture.



**Fig. 9** Fracture rate of points of interest on deposit under 1.8-MPa steam pressure

### 4.3 Effect of different sootblowing pressures on deposit failure

Sootblowing pressure is an essential parameter for this simulation, and high sootblowing pressure can easily destroy the deposit. High-pressure steam can also erode the wall tube surface and consume additional steam. Hence, the extent of deposit fracture was compared through  $\eta_t$ -time curves under different sootblowing pressures, as shown in Fig. 10. Under different sootblowing pressures of 0.9–1.8 MPa, sootblowing yields different dynamic features of deposit failure. Although the results of deposit failure show similar tendencies, high sootblowing pressures lead to rapid deposit cracking. The deposit fails at 1 ms when the sootblowing pressure is 1.8 MPa. However, deposit failure occurs slowly at the pressure of 0.9 MPa, and a long sootblowing time of over 1.4 ms is necessary. The  $\eta_t$ -time curves nearly coincide for



pressures of 1.5 MPa and 1.2 MPa, which implies similar deposit failure dynamics.

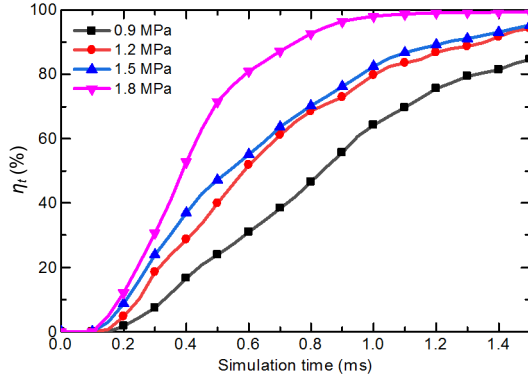


Fig. 10 Extent of deposit failure under different sootblowing pressures

Wall tube steel can be exposed to high-pressure sootblowing steam if the slag deposit is broken and falls off, thereby adversely affecting steel safety and its lifetime. Wall tube leaks may also occur. Thus, the wall tube stress due to sootblowing (SWS) was examined to evaluate the effects of sootblowing on the steel lifetime. Therefore, the maximum SWS (MSWS) on the windward side was calculated as shown in Fig. 11. Another parameter concerning sootblowing is steam consumption, which is closely related to economic benefits. Therefore, the mass of steam consumption per wall tube surface,  $V$ , was adopted, which can be expressed as

$$V = v_{\text{avg}} \cdot t_{\eta 80\%} \cdot \rho_{\text{steam}} \cdot \frac{S_{\text{jet}}}{S_{\text{tube}}}, \quad (12)$$

where  $v_{\text{avg}}$  denotes the average entrance velocity of sootblowing steam flow,  $t_{\eta 80\%}$  is the sootblowing time corresponding to  $\eta_t = 80\%$ ,  $\rho_{\text{steam}}$  is the density of steam,  $S_{\text{jet}}$  is the exit area of the sootblower nozzle jet, and  $S_{\text{tube}}$  is the area of the wall tube surface.

As shown in Fig. 11, the MSWS steadily increases with the sootblowing pressure. However, steam consumption costs fluctuate with the pressure. Although steam consumption is the least when the sootblowing pressure is 1.8 MPa, the MSWS reaches about 24 MPa during sootblowing, which can cause serious material erosion. In contrast, MSWS is the lowest when the sootblower pressure is 0.9 MPa; however,

more steam is consumed than that in the high-pressure cases. Given that the steam jets at 1.2 MPa and 1.5 MPa achieve similar deposit failures, the 1.2-MPa steam pressure is selected upon considering the factors of MSWS and  $V$ . When the pressure value of 1.2 MPa is adopted, MSWS is approximately 13 MPa,  $V$  is  $0.14 \text{ kg/m}^2$ , and the necessary sootblowing time is 1.1 ms. Therefore, this set of sootblowing parameters was suitable and economical for boiler operation.

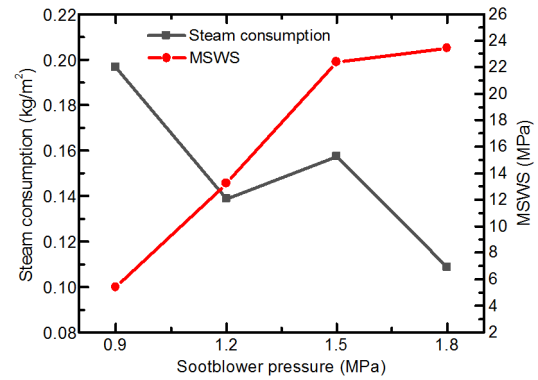


Fig. 11 Steam consumption and MSWS under various sootblower pressures

## 5 Conclusions

To replicate the dynamic failure of ash deposit under steam sootblowing, we developed a novel numerical model of deposit and steam flow in ABAQUS through CZM and CEL analysis. The dynamic details and mechanism of deposit failure by steam sootblowing were revealed by the proposed model. The destructive degree of the deposit and the scalar stiffness degradation variable were obtained to measure the dynamic destructive status during sootblowing. The fracture mechanism was revealed by fracture rate analysis of the ash deposit. The spread of transverse normal tension caused by steam jets was the primary contributor to deposit fracture, and direct steam impact on the deposit formed the initial source of transverse normal tension, which played a subsidiary role after initiation of the deposit fracture.

The effects of the sootblowing pressure on the deposit were studied contrastively in the range of 0.9–1.8 MPa. The damage degree of deposit, steam consumption, and MSWS were chosen as representative effects of the sootblowing pressure. In general,

the deposit began to break nearly simultaneously for all pressures, and subsequently, the breaking process firstly presented an accelerated tendency followed by a decelerated one. Higher sootblowing pressure led to quicker deposit fracture, and the deposit failure was complete over 1.0–1.5 ms due to different pressures. The simulation results indicated that the sootblowing pressure of 1.2 MPa was suitable and economical for boiler/furnace operation.

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## 中文概要

**题目：**蒸汽吹灰过程中水冷壁渣层破坏过程的模拟分析

**目的：**蒸汽吹灰是锅炉运行中常见的破坏水冷壁渣层的方法。本文通过建立三维吹灰模型，模拟不同压力下吹灰过程中蒸汽射流和渣层破坏的动态变化过程，研究在渣层破坏过程中应力波的传播变化，得出条件合适的吹灰参数。

**创新点：**1. 通过内聚力单元法和耦合欧拉-拉格朗日法建立吹灰流程的三维数值模型，详细揭示渣层破坏的动力学过程，并对蒸汽射流的扩散和应力波在渣层中的传播进行全过程分析；2. 通过建立三维数值模拟，研究吹灰蒸汽压力对渣层破坏、管壁应力 and 蒸汽消耗的影响，并通过模拟结果探讨合适的吹灰参数。

**方法：**1. 对渣层模型采用内聚力单元法进行建模；2. 对蒸汽射流和渣层的流固耦合现象采用 ABAQUS 中的耦合欧拉-拉格朗日法进行分析。

**结论：**1. 越高的吹灰压力会导致渣层被破坏得越快并最终完全脱离水冷壁；综合考虑渣层破坏效率、水冷壁管应力 and 蒸汽消耗的影响，1.2 MPa 是最合适和经济的吹灰压力参数。2. 蒸汽射流带来的切向应力是引起渣层破坏的主要因素，射流对渣层的直接冲击是切向应力的来源，并且是渣层破坏的次要因素。

**关键词：**吹灰；锅炉；数值模型；内聚力单元法；渣层破坏